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edited by Ling-Lie Chau and Werner Nahm

# Differential Geometric Methods in Theoretical Physics

## Physics and Geometry

Edited by

Ling-Lie Chau and Werner Nahm

University of California, Davis  
Davis, California

Proceedings of the NATO Advanced Research Workshop  
and the 18th International Conference on  
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## CONTENTS

<i>Introduction to the 18th Conference on 'Differential Geometrical Methods in Theoretical Physics'</i> .....	1	<i>Cyclic Cohomology, Supersymmetry and KMS States</i> <i>The KMS States as Generalized Elliptic Operators</i> .....	105
K. Bleuler		D. Kastler	
<b>(1) Integrable Systems</b>		<i>Symmetrics of Quantum Space, Braid Representation, and Classification of Subfactors</i> .....	117
<i>Baxterization</i> .....	5	A. Ocneanu	
V.F.R. Jones		<i>New Kinematics (Statistics and Symmetry) in Low-Dimensional QFT with Applications to Conformal QFT<sub>2</sub></i> .....	119
<i>Geometric Classification of Commutative Algebras of Ordinary Differential Operators</i> .....	13	B. Schroer	
M. Mulase		<i>Infinite Index Embeddings</i> .....	145
<i>Geometrical Aspects of Solvable Two Dimensional Models</i> .....	29	R. Herman	
K. Tanaka		<b>(3) Conformal Field Theory</b>	
<i>Explicit Soliton-Generating Bäcklund Transformations</i> .....	41	<i>Non-Compact Current Algebras and Heterotic Superstring Vacua</i> .....	147
H.-C. Yen and J.C. Shaw		I. Bars	
<i>Integrability Conditions: Recent results in the theory of integrable models</i> .....	47	<i>Aspects of Perturbed Conformal Field Theory, Affine Toda Field Theory and Exact S-Matrices</i> .....	169
R. Bullough, S. Olafsson, Yu-Zhong Chen, and J. Timonen		H.W. Braden, E. Corrigan, P.E. Dorey, and R. Sasaki	
<i>Nonlinear Differential Equations in Physics and Their Geometrical Integrability Properties</i> .....	71	<i>Codes, Lattices and Conformal Field Theory</i> .....	183
L.-L. Chau		P. Goddard	
<i>Integrability Off Criticality and Quantum Integrable Systems</i> .....	79	<i>Topics on Conformal Field Theory</i> .....	185
P. Mathieu		C. Itzykson	
<i>Quantization of the Chiral Solitonic Bag Model</i> .....	87	<i>Feigin-Fuchs Representation of Conformal Field Theory</i> .....	187
N.K. Pak and T. Yilmaz		D. Nemeschansky	
<b>(2) Operator Algebras</b>		<i>Coulomb-Gas Construction on Higher-Genus Riemann Surfaces</i> .....	189
<i>Structure of Superselection Sectors in Low-Dimensional Quantum Field Theory</i> .....	95	J. Bagger and M. Goulian	
K. Fredenhagen		<i>Conformal Algebras and Non-linear Differential Equations</i> .....	203
		I. Bakas	
		<i>S Matrices of the Tricritical Ising Model and Toda Systems</i> .....	213
		P. Christe	
		<i>Quantum Groups, Braiding Matrices and Coset Models</i> .....	223
		H. Itoyama	
		<i>Gauged WZW Models and the Coset Construction of Conformal Field Theories</i> .....	237
		D. Karabali	
		<i>Flat Connection, Conformal Field Theory and Quantum Group</i> .....	251
		M. Kato	
		<i>Classical and Quantum Calabi-Yau Manifolds</i> .....	257
		R. Schimmrigk	
		<i>Conformal Field Theories and Category Theory</i> .....	271
		R. Brustein, Y. Ne'eman, and S. Sternberg	

<i>Quantum Bäcklund Transformations and Conformal Algebras</i> .....	279	<i>Progress in Multi-Genus Calculations for the Spinning String</i> .....	445
T. Curtright		A. Parkes	
<i>A Coset-Construction for Integrable Hierarchies</i> .....	291	<i>The Minimal Set of the Generators of Dehn Twists on a High Genus</i>	
F.A. Bias and K. de Vos		<i>Riemann Surface</i> .....	455
<i>Away From Criticality: Some Results From the S Matrix Approach</i> .....	297	C.-Z. Zha	
G. Mussardo		<i>Strings and Teichmueller Space</i> .....	465
<i>Normal Ordered Products and Parafields in Conformal Field Theory</i> .....	309	K. Bugajska	
W. Nahm		<i>Holomorphic Differentials on Punctured Riemann Surfaces</i> .....	475
<i>Chiral Gauge Field Theory in Two Dimensions</i> .....	315	R. Dick	
J. Quackenbush		<i>Anomalies, BRS Symmetry and Superconnections</i> .....	485
<i>Monodromy Properties of Conformal Field Theories and Quantum Groups</i> .....	323	A.C. Hirshfeld	
P. Valtancoli		<i>General Covariance and Strings</i> .....	493
(4) <b>Quantum Groups</b>		F.R. Klinkhamer	
<i>Matrix elements of unitary representations of the quantum</i>		<i>Spontaneous Symmetry Breaking in 4-Dimensional Heterotic String</i> .....	497
<i>group <math>SU_q(1,1)</math> and the basic hypergeometric functions</i> .....	331	J. Maharana	
K. Ueno, T. Masuda, K. Mimachi, Y. Nakagami, M. Noumi, and Y. Saburi		<i>Superghost Fields in <math>N = 2</math> Superconformal Algebra</i> .....	505
<i>A <math>q</math>-Analogue of the Lie Superalgebra <math>OSp(2,1)</math> and its</i>		S. Nam	
<i>Metaplectic Representation...</i> .....	345	(6) <b>Topological QFT</b>	
C. Devchand		<i>Topological Quantum Field Theories: Relations Between Knot Theory and</i>	
<i><math>q</math>-Deformation of <math>SU(1,1)</math> Conformal Ward Identities and <math>q</math>-Strings</i> .....	353	<i>Four Manifold Theory</i> .....	513
A. LeClair		B. Grossman	
<i><math>Q</math>-Deformation of <math>sl(2, c) \times Z_N</math> and Link Invariants</i> .....	359	<i>Topological Quantum Theories and Representation Theory</i> .....	533
H.C. Lee		P. Woit	
<i>Quantum Group Duality in Vertex Models and Other Results in</i>		<i>Topological Chern-Simons Gauge Theories and "New" Knot/Link Polynomials</i> ..	547
<i>the Theory of Quasitriangular Hopf Algebras</i> .....	373	Y.-S. Wu	
S. Majid		<i>Observables in Topological Yang-Mills Theory and the Gribov Problem</i> .....	563
(5) <b>Strings</b>		H. Kanno	
<i>Physics at the Planck Length and <math>p</math>-Adic Field Theories</i> .....	387	<i>Linking the Gauss-Bonnet-Chern Theorem, Essential Hopf Maps and</i>	
I.Y. Aref'eva		<i>Membrane Solitons with Exotic Spin and Statistics</i> .....	571
<i>Non-Archimedean Geometry and Applications to Particle Theory</i> .....	399	C.-H. Tze	
P.H. Frampton		<i>Moduli Spaces and Topological Quantum Field Theories</i> .....	585
<i>Beyond Conformal Field Theory</i> .....	409	J. Sonnenschein	
P. Nelson		<i>Knots in Physics</i> .....	593
<i>Hidden Symmetries of Strings and Their Relevance for</i>		M.U. Werner	
<i>String Quantization</i> .....	415	(7) <b>Geometry and Supergeometry</b>	
K. Pohlmeyer		<i>Supermanifold, Symplectic Structure and Geometric Quantization</i>	
<i>Hamiltonian Flows, <math>SU(\infty)</math>, <math>SO(\infty)</math>, <math>US_p(\infty)</math>, and Strings</i> .....	423	<i>of BRST Systems</i> .....	603
C. Zachos		S.-M. Fei, H.-Y. Guo, and Y. Yu.	
<i>A Geometric Approach To The String BRS Cohomology</i> .....	431	<i>Ambitwistors and Conformal Gravity</i> .....	621
H. Aratyn		C. LeBrun	

<i>Toward Classification of Classical Lie Superalgebras</i> .....	633	<i>Principal Bundles Versus Lie Groupoids in Gauge Theory</i> .....	793
D.A. Leites		M.E. Mayer	
<i>Status of the Algebraic Approach to Super Riemann Surfaces</i> .....	653	<i>Static and Axially Symmetric Soliton Solutions to the Self-Dual <math>SU(3)</math></i>	
J.M. Rabin		<i>and <math>SU(2)</math> Gauge Fields in a Euclidean Space</i> .....	803
<i>Projective Embeddings of Complex Supermanifolds</i> .....	669	D.B. Papadopoulos	
R.O. Wells		<i>Superalgebra and Superspace of Vector Spinor Generators</i> .....	813
<i>Some Results on Line Bundles over SUSY-Curves</i> .....	675	S. Rajpoot	
C. Bartocci, U. Bruzzo, and D. Hernández Ruipérez		<i>Participants</i> .....	819
<i>Instantons From Supersymmetric Conformal Chiral Scalar</i>		<i>Author Index</i> .....	827
<i>Superfield Theories</i> .....	681	<i>Subject Index</i> .....	829
S. Catto			
<i>Einstein-Hermitian Bundles over Complex Surfaces</i> .....	689		
F.J. Flaherty			
<i>Symplectic Reduction of the Minimally Coupled Massless</i>			
<i>Superparticle in <math>D=10</math></i> .....	693		
J. Harnad, J.A. Shapiro, S. Shnider, and C.C. Taylor.			
 (8) Gravity			
<i>Quantum Gravity and the Berry Phase</i> .....	703		
G. Venturi			
<i>Gravity and Lorentz Breakdown in Higher-Dimensional</i>			
<i>Theories and Strings</i> .....	715		
V.A. Kostelecky and S. Samuel			
<i>Current Algebra and Extended 2D Gravity With Higher Spin Gauge Field</i> .....	727		
Y. Matsuo			
<i>The Parametric Manifold Picture of Space-Time</i> .....	741		
Z. Perjés			
<i>Gravity as an <math>SO(3,2)</math> Gauge Theory</i> .....	757		
S. Gotzes			
 (9) Others			
<i>Heuristics of Solitary Waves in Non-Integrable Field Theories</i> .....	767		
D.K. Campbell			
<i>Lattice Approach of the Antiferromagnetic Heisenberg Model</i>			
<i>in 2+1 Dimensions and the Hopf Chern-Simons Terms</i> .....	769		
W.-Z. Li			
<i>Is It Possible To Do Canonical Quantum Field Theory Rigorously?</i> .....	779		
R.N. Sen			
<i>A Global Theory of Parametrized Quantum Mechanics</i> .....	787		
L.N. Chang and Y. Liang			